#### MATHEMATICS



# QUESTION PAPER

#### Time Allowed : 2 hrs 30 min

#### Total Marks: 300

#### Instructions

- 1. This Test Booklet contains **120** items (questions). Each item is printed in **English**. Each item comprises four responses (answers). You will select the response which you want to mark on the Answer Sheet. In case you feel that there is more than one correct response, mark the response which you consider the best. In any case, choose **ONLY ONE** response for each item.
- 2. You have to mark all your responses **ONLY** on the separate Answer Sheet provided. See directions in the Answer Sheet.
- 3. All items carry equal marks.
- 4. Before you proceed to mark in the Answer Sheet the response to the various items in the Test Booklet, you have to fill in some particulars in the Answer Sheet as per instructions.
- 5. Penalty for wrong answers : THERE WILL BE PENALTY FOR WRONG ANSWERS MARKED BY A CANDIDATE IN THE OBJECTIVE TYPE QUESTION PAPERS.
  - (i). There are four alternatives for the answer to every question. For each question for which a wrong answer has been given by the candidate, **one-third** of the marks assigned to that question will be deducted as penalty.
  - (ii). If a candidate gives more than one answer, it will be treated as a *wrong answer* even if one of the given answers happens to be correct and there will be same penalty as above to that question.
  - (iii). If a question is left blank, i.e., no answer is given by the candidate, there will be **no penalty** for that question.
- **1.** If the sum of binomial coefficients in the expansion of  $(x + y)^n$  is 256, then the greatest binomial coefficient occurs in which one of the following terms?

(a) Third (b) Fourth (c) Fifth (d) Ninth

**2.** If  $k < (\sqrt{2} + 1)^3 < k + 2$ , where *k* is a natural number, then what is the value of *k*? (a) 11 (b) 13 (c) 15 (d) 17

(a) 11 (b) 13 (c) 15 (d)  
3. If 
$$\begin{bmatrix} x & 1 & 1 \end{bmatrix} \begin{bmatrix} 1 & 2 & 3 \\ 4 & 5 & 6 \\ 7 & 8 & 9 \end{bmatrix} \begin{bmatrix} 1 \\ 1 \\ x \end{bmatrix} = \begin{bmatrix} 45 \end{bmatrix}$$

then which one of the following is a value of x? (a) -2 (b) -1 (c) 0 (d) 1

4. If 
$$A = \begin{bmatrix} y & z & x \\ z & x & y \\ x & y & z \end{bmatrix}$$

Where *x*, *y* and *z* are integers, is an orthogonal matrix, then what is the value of  $x^2 + y^2 + z^2$ ?

- **5.** Consider the following in respect of a non-singular matrix *M*:
  - I.  $|M^2| = |M|^2$
  - **II.**  $|M| = |M^{-1}|$

**I.** 
$$|M| = |M^T|$$

How many of the above are correct?

(a) None (b) One (c) Two (d) All three

6. If 
$$f(\theta) = \begin{bmatrix} \cos \theta & \sin \theta \\ -\sin \theta & \cos \theta \end{bmatrix}$$
 then what is  $(f(\pi))^2$ 

(a) 
$$\begin{bmatrix} -1 & 0 \\ 0 & -1 \end{bmatrix}$$
 (b)  $\begin{bmatrix} 1 & 1 \\ 1 & 1 \end{bmatrix}$   
(c)  $\begin{bmatrix} -1 & 0 \\ 0 & 1 \end{bmatrix}$  (d)  $\begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$   
7. If  $A = \begin{bmatrix} 1 & 2 & 2 \\ 2 & 1 & 2 \\ 2 & 2 & 1 \end{bmatrix}$  then what is  $A^2 - 4A$  equal to?

(a)  $-5I_3$  (b)  $-I_3$  (c)  $I_3$  (d)  $5I_3$ 

Where  $I_3$  is the identity matrix of order 3.

8. If the number of selections of r as well as (n + r) things from 5n different things are equal, then what is the value of r?

(a) 
$$n$$
 (b)  $2n$  (c)  $3n$  (d)  $4n$ 

- **9.** What is the number of selections of at most 3 things from 6 different things?

(a) 20 (b) 22 (c) 41 (d) 42 
$$\begin{bmatrix} x & y & z \end{bmatrix}$$

- **10.** If  $A = \begin{vmatrix} y & z & x \\ z & x & y \end{vmatrix}$  where *x*, *y* and *z* are integers
  - is an orthogonal matrix, then what is  $A^2$  equal to?
  - (a) Null matrix (b) Identity matrix
  - (c) A (d) –A

**Direction for Questions (11-13):** Consider the following for the three (03) items that follow: Let  $p = \tan 2\alpha - \tan \alpha$  and  $q = \cot \alpha - \cot 2\alpha$ .

equal to?

**11.** What is (p/q) equal to? (a)  $-\tan \alpha \tan 2\alpha$  (b)  $-\cot \alpha . \cot 2\alpha$ (c)  $\tan \alpha . \tan 2\alpha$  (d)  $\cot \alpha . \cot 2\alpha$  **12.** What is (p + q) equal to? (a)  $\sec 4\alpha$  (b)  $\csc 4\alpha$ (c)  $2\sec 4\alpha$  (d)  $2\csc 4\alpha$  **13.** What is  $\tan^2 \alpha$  equal to? (u)  $2\pi \cos^2 4\alpha$ 

(a) 
$$\frac{(pq)}{(p+q)}$$
 (b)  $\frac{(p+2q)}{p}$   
(c)  $\frac{p}{(p+2q)}$  (d)  $\frac{p}{(2p+q)}$ 

**Direction for Questions (14-15):** Consider the following for the two (02) times that follow: Let  $2\sin \alpha + \cos \alpha = 2$ , where  $0 < \alpha < 90^{\circ}$ 

- **14.** What is  $\tan \alpha$  equal to?
  - (a)  $\frac{1}{2}$  (b) 1 (c)  $\frac{3}{4}$  (d) 2
- **15.** What is  $2 \sin 2\alpha + \cos 2\alpha$  equal to?

(a) 
$$\frac{11}{10}$$
 (b)  $\frac{11}{5}$  (c)  $\frac{12}{5}$  (d)  $\frac{13}{5}$ 

**Direction for Questions (16-17):** Consider the following for the two (02) times that follow: In a triangle *ABC*, two sides *BC* and *CA* are in the ratio 2 : 1, and their opposite corresponding angles are in the ratio 3 : 1.

16. One of the angles of the triangle is

(a) 15°	(b)	30°
(c) 45°	(d)	75°

- **17.** Consider the following statements:
  - **I.** The triangle is right-angled.
  - **II.** One of the sides of the triangle is 3 times the other.
  - **III.** The angles *A*, *C* and *B* of the triangle are in *AP*.

Which of the statements give above is/are correct?

- (a) I only (b) II and III only
- (c) I and III only (d) I, II and III
- **18.** A man at *M* standing 100 m away from the base (P) of a chimney of height 50 m. He observes the angle of elevation of the highest point (Q) of the smoke to be 45°. The highest point of the chimney is at *R*. Further *P*, *R* and *Q* are in a straight line and the straight line is perpendicular to PM. What is the angle RMQ equal to?
  - (a)  $\tan^{-1}\left(\frac{1}{2}\right)$  (b)  $\tan^{-1}\left(\frac{1}{3}\right)$ (c)  $\tan^{-1}\left(\frac{2}{3}\right)$  (d)  $\tan^{-1}\left(\frac{3}{4}\right)$

**19.** If *k* is a root of  $x^2 - 4x + 1 = 0$ , then what is  $\tan^{-1} k + \tan^{-1} \frac{1}{k}$  equal to?

(a) 
$$\frac{-\pi}{2}$$
 (b) 0 (c)  $\frac{\pi}{4}$  (d)  $\frac{\pi}{2}$ 

**20.** If  $\tan^{-1} k + \tan^{-1} \frac{1}{2} = \frac{\pi}{4}$ 

(a) 1 (b)  $\frac{1}{2}$  (c)  $\frac{1}{3}$  (d)  $\frac{1}{4}$ 

- **21.** If a line in 3 dimensions makes angles  $\alpha$ ,  $\beta$  and  $\gamma$  with the positive directions of the coordinate axes, then what is  $\cos(\alpha + \beta) \cos(\alpha \beta)$  equal to?
  - (a)  $\cos^2 \gamma$  (b)  $-\cos^2 \gamma$ (c)  $\sin^2 \gamma$  (d)  $-\sin^2 \gamma$
- **22.** A(1, 2, -1), B(2, 5, -2) and C(4, 4, -3) are three vertices of a rectangle. What is the area of the rectangle?
  - (a) 8 square units
  - (b) 9 square units
  - (c)  $\sqrt{66}$  square units

(d)  $\sqrt{68}$  square units

**23.** *ABC* is a triangle right-angled at *B*. If A(k, 1, -1), B(2k, 0, 2) and C(2 + 2k, k, 1) are the vertices of the triangle, then what is the value of *k*? (a) -3 (b) -1 (c) 1 (d) 3

24. If a line 
$$\frac{x+1}{p} = \frac{y-1}{q} = \frac{z-2}{r}$$

Where p = 2q = 3r makes an angle with the position direction of the *y*-axis then what is  $\cos 2\theta$  equal to?

(a) 
$$\frac{-31}{49}$$
 (b)  $\frac{-37}{49}$  (c)  $\frac{31}{49}$  (d)  $\frac{37}{49}$ 

25. What is the equation of the plane passing through the point (1, 1, 1) and perpendicular to the line whose direction ratio is (3, 2, 1)?
(a) x + 2y + 3z = 6
(b) 3x + 2y + z = 6
(c) x + y + z = 3

(d) 
$$3x + 2y + z = 0$$

**26.** A line makes angles  $\alpha$ ,  $\beta$  and  $\gamma$  with the positive directions of the coordinate axes.

If  $\vec{a} = (\sin^2 \alpha)\hat{i} + (\sin^2 \beta)\hat{j} + (\sin^2 \gamma)\hat{k}$  and

$$\vec{b} = \hat{i} + \hat{j} + \hat{k}$$
 then what is  $\vec{a}.\vec{b}$  equal to?

a) 
$$-2$$
 (b)  $-1$  (c) 1 (d) 2

- 27. Consider the following statements with respect to a vector  $\vec{d} = (\vec{a} \times \vec{b}) \times \vec{c}$ :
  - **I.**  $\vec{d}$  is coplanar with  $\vec{a}$  and  $\vec{d}$
  - **II.**  $\vec{d}$  is perpendicular to  $\vec{c}$

Which of the statements given above is/are correct? (a) I only (b) II only (c) Both I and II (d) Neither I nor II 28. The position vectors of three points A, B and C are  $\vec{a}, \vec{b}$  and  $\vec{c}$ , respectively, such that  $3\vec{a} - 4\vec{b} + \vec{c} = \vec{0}$ . What is AB : BC equal to? (a) 3:1 (b) 1:3(c) 3:4 (d) 1:429. The position vectors of three points A, B and C are  $\vec{a}.\vec{b}$  and c respectively, where,

 $\vec{c} = (\cos^2 \theta)\vec{a} + (\sin^2 \theta)\vec{b}$ . What is  $(\vec{a} \times \vec{b}) + (\vec{b} \times \vec{c}) + (\vec{b} \times \vec{c})$ 

 $(\vec{c} \times \vec{a})$  equal to?

- (a)  $\vec{o}$ (b)  $2\vec{c}$ (c) 3c(d) unit vector
- **30.** Let  $\vec{a}, \vec{b}$  and  $(\vec{a} \times \vec{b})$  be unit vectors. What is
  - (a.b) equal to? (b)  $\frac{1}{2}$ **(a)** 0 (c) 1 (d) 3
- **31.** The sum of the first *k* terms of a series is  $3k^2 + 5k$ . Which one of the following is correct?
  - (a) The terms of S form an arithmetic progression with common difference 14.
  - (b) The terms of S form an arithmetic progression with common difference 6.
  - (c) The terms of S form a geometric progression with a common ratio  $\frac{10}{7}$
  - (d) The terms of S form a geometric progression with a common ratio  $\frac{11}{4}$
- **32.** The sum of the first 8 terms of a GP is 5 times the sum of its first 4 terms. If  $r \neq 1$  is the common ratio, then what is the number of possible real values of k?
  - (a) One (b) Two

**33.** If one root of the equation  $x^2 - kx + k = 0$ exceeds the other by  $2\sqrt{3}$  then which one of the following is a value of  $k^2$ 

the follow	ing is a value of r	
(a) 3	(b)	6
(c) 9	(d)	12

34. If  $x + \frac{5}{y} = 4$  and  $y + \frac{5}{x} = -4$ , then what is (x + y)equal to?

- **35.** If the 5<sup>th</sup>, 7<sup>th</sup> and 13<sup>th</sup> terms of an *AP* are in *GP*, then what is the ratio of its first term to its common difference?
  - (a) -3 **(b)** –2 (d) 3 (c) 2

- **36.** If *p*, 1 and *q* are in *AP* and *p* and 2 *q* are in *GP*, then which of the following statements is/are correct?
  - *p*, 4, *q* are in HP. I.
  - $\left(\frac{1}{p}\right), \frac{1}{4}, \left(\frac{1}{q}\right)$  are in AP. II.

Select the answer using the code given below:

- (a) I only (b) II only
- (c) Both I and II (d) Neither I nor II
- **37.** If  $x = (1111)_2$ ,  $y = (1001)_2$  and  $z = (110)_2$ , then what is  $x^3 - y^3 - z^3 - 3xyz$  equal to? (a)  $(1111001)_2$  (b)  $(1001111)_2$ (c)  $(1)_2$  (d)  $(0)_2$ **38.** If  $\Delta = \begin{bmatrix} a & b & c \\ d & e & f \\ g & h & i \end{bmatrix}$  and *A*, *B*, *C*, *D* and *G* are (c) (1)<sub>2</sub>

the cofactors of the elements a, b, c, d and g respectively, then what is bB + cC - dD - gGequal to?

(a) 0 **(b)** 1 (c) Δ (d)  $-\Delta$ **39.** Consider the following statements in respect of

 $k(k+2) \quad 2k+1 \quad 1$ the determinant  $\Delta = \begin{bmatrix} 2k+1 \\ 3 \end{bmatrix}$ 

**I.**  $\Delta$  is positive if k > 0.

**II.**  $\Delta$  is negative if k < 0.

**III.**  $\Delta$  is zero if k = 0.

- How many of the statements given above are correct?
- (a) None (b) One (c) Two (d) All three
- 2 3+i 1  $0 \quad i-1 = A + iB \text{ where } i = \sqrt{-1}$ **40.** If |3-i|1 -1 -1-i

then what is A + B equal to? (a) -10 (b) -6(c) 0 (d) 6 Direction for Questions (41-43): Consider the following for the three (03) items that follow:

- Let  $p = \sin 35^\circ$ ,  $q = \sin 25^\circ$  and  $r = \sin(-95^\circ)$ . **41.** What is (p + q + r) equal to? **(b)** 0 (c) 2sin 5° (d) 2cos 5° (a) -1
- **42.** What is (pq + qr + rp) equal to?

(a) 
$$\frac{-3}{4}$$
 (b) 0 (c)  $\frac{1}{4}$  (d)  $\frac{3}{4}$ 

**43.** What is 
$$(p^2 + q^2 + r^2)$$
 equal to?  
(a)  $\frac{1}{2}$  (b) 1 (c)  $\frac{3}{2}$  (d) 2

Direction for Questions (44-45): Consider the following for the two (02) items that follow: Let  $p = [\sin \alpha - \sin(\alpha - 90^\circ)].$ 

**44.** What is the minimum value of *p*?

(a) 0 (b) 
$$\frac{1}{2}$$
 (c)  $\frac{1}{\sqrt{2}}$  (d) 1

**45.** What is the maximum value of *p*?

(a) 1 (b)  $\sqrt{2}$  (c)  $\sqrt{3}$  (d) 2 **Direction for Questions (46-48):** Consider the following for the three (03) items that follow: The sides of a triangle *ABC* are *AB* = 3 cm, *BC* = 5 cm and *CA* = 7 cm.

- 46. Consider the following statements:
  - I. The triangle is an obtuse-angled triangle.
  - **II.** The sum of acute angles of the triangle is also acute.

Which of the statements given above is/are correct?

- (a) I only (b) II only
- (c) Both I and II (d) Neither I nor II **47.** What is  $\angle B$  equal to?
- (a)  $60^{\circ}$  (b)  $105^{\circ}$  (c)  $120^{\circ}$  (d)  $150^{\circ}$
- **48.** What is the area of the area of the triangle?

(a) 
$$\frac{15\sqrt{3}}{4}$$
 square cm (b)  $\frac{15\sqrt{3}}{2}$  square cm

(c) 
$$15\sqrt{3}$$
 square cm (d)  $30\sqrt{3}$  square cm

**Direction for Questions (49-50):** Consider the following for the two (02) items that follow: The top (M) of a tower is observed from three points P, Q and R lying in a horizontal straight line which passes directly a long the foot (N) of the tower. The angles of elevations of M from P, Q and R are 30°, 45° and 60°, respectively. Let PQ = a and QR = b.

**49.** What is *PN* equal to?

(a) 
$$\left(\frac{3-\sqrt{3}}{2}\right)a$$
 (b)  $\left(\frac{3+\sqrt{3}}{2}\right)a$   
(c)  $\left(\frac{3-\sqrt{3}}{4}\right)a$  (d)  $\left(\frac{3+\sqrt{3}}{4}\right)a$ 

50. What is MN equal to?

(a) 
$$\left(\frac{3+\sqrt{3}}{2}\right)b$$
 (b)  $\left(\frac{3-\sqrt{3}}{2}\right)b$   
(c)  $\left(\frac{3-\sqrt{3}}{4}\right)b$  (d)  $\left(\frac{3+\sqrt{3}}{4}\right)b$ 

**Direction for Questions (51-52):** Consider the following for the two (02) items that follow:

The probabilities that A, B and C become managers are  $\frac{3}{10}$ ,  $\frac{1}{2}$  and  $\frac{4}{5}$ , respectively. The probabilities that the bonus scheme will be introduced if A, B and C become managers are  $\frac{4}{9}$ ,  $\frac{2}{9}$  and  $\frac{1}{3}$ , respectively.

**51.** What is the probability that the bonus scheme will be introduced?

(a) 
$$\frac{17}{45}$$
 (b)  $\frac{19}{45}$  (c)  $\frac{23}{45}$  (d)  $\frac{26}{45}$ 

**52.** If the bonus scheme has been introduced, then what is the probability that the manager appointed was B?

(a) 
$$\frac{5}{23}$$
 (b)  $\frac{6}{23}$  (c)  $\frac{7}{23}$  (d)  $\frac{8}{23}$ 

- 53. The arithmetic mean of 100 observations is 50. If 5 is subtracted from each observation and then divided by 20, then what is the new arithmetic mean?
  (a) 2.25 (b) 3.5 (c) 4.25 (d) 5.5
- 54. The standard deviation of 100 observations is 10. If 5 is added to each observation and then divided by 20, then what will be the new standard deviation?
  (a) 0.25 (b) 0.5 (c) 0.75 (d) 1.00

55. If 
$$P(A) = \frac{1}{3}$$
,  $P(B) = \frac{1}{2}$  and  $P(A \cap B) = \frac{1}{4}$ , then  
what is the value of  $P(B|A^c)$ ?  
(a)  $\frac{1}{8}$  (b)  $\frac{3}{8}$  (c)  $\frac{5}{8}$  (d)  $\frac{7}{8}$ 

56. If 
$$P(A) = \frac{1}{3}$$
,  $P(B) = \frac{1}{2}$  and  $P(A \cap B) = \frac{1}{4}$ ,

then what is the value of  $P(A^c \cap B^c)$ ?

(a) 
$$\frac{1}{4}$$
 (b)  $\frac{5}{12}$  (c)  $\frac{7}{12}$  (d)  $\frac{11}{12}$ 

**57.** If two fair dice are tossed then what is the probability that the sum of the numbers on the faces of the dice is strictly greater than 7?

(a) 
$$\frac{1}{3}$$
 (b)  $\frac{5}{12}$   
(c)  $\frac{7}{12}$  (d)  $\frac{3}{4}$ 

**58.** The probability of a man hitting a target is  $\frac{1}{5}$ . If the man fires 7 times, then what is the

probability that he hits the target at least twice?

(a) 
$$1 - \left(\frac{3}{5}\right) \left(\frac{4}{5}\right)^6$$
 (b)  $1 - \left(\frac{3}{5}\right) \left(\frac{4}{5}\right)^7$   
(c)  $1 - \left(\frac{11}{5}\right) \left(\frac{4}{5}\right)^6$  (d)  $1 - \left(\frac{11}{5}\right) \left(\frac{4}{5}\right)^7$ 

**59.** Let *X* be a random variable following binomial distribution whose mean and variance are 200 and 160, respectively. What is the value of the number of trials (*n*)?

(a) 500 (b) 1000 (c) 1500 (d) 2000

**60.** What is the arithmetic mean of  $8^2$ ,  $9^2$ ,  $10^2$ , ...  $15^2$ ?

(a) 133.5 (b) 135.5 (c) 137.5 (d) 139.5 Direction for Questions (61-62): Consider the following for the two (02) items

Let 
$$y = \sin^{-1}\left(x - \frac{4x^3}{27}\right)$$

**61.** What is *y* equal to?

(a) 
$$\sin^{-1} x$$
 (b)  $\sin^{-1} \left(\frac{x}{3}\right)$   
(c)  $3\sin^{-1} x$  (d)  $3\sin^{-1} \left(\frac{x}{3}\right)$ 

**62.** What is  $\frac{dy}{dx}$  equal to?

(a) 
$$\frac{1}{\sqrt{9-x^2}}$$
 (b)  $\frac{1}{\sqrt{3-x^2}}$   
(c)  $\frac{3}{\sqrt{9-x^2}}$  (d)  $\frac{9}{\sqrt{9-x^2}}$ 

**Direction for Questions (63-64):** Consider the following for the two (02) items that follow: Let the function  $f(x) = x^2 + 9$ .

63. What if 
$$\lim_{x \to 0} \frac{\sqrt{f(x)} - 3}{\sqrt{f(x) + 7} - 4}$$
 equal to?  
(a)  $\frac{2}{3}$  (b) 2 (c)  $\frac{4}{3}$  (d) 2

**64.** Consider the following statements:

I. f(x) is an increasing function.

II. f(x) has local maximum at x = 0

Which of the statements given above is/are correct?

(a) I only (b) II only

(c) Both I and II (d) Neither I nor II Direction for Questions (65-66): Consider the following for the two (02) items that follow:

The function 
$$f(x)$$
 satisfies  $f\left(\frac{x}{y}\right) = \frac{f(x)}{f(y)}$  for all

positive real values of *x* and *y*, and f(2) = 3

65. What is f(16) equal to?
(a) 18 (b) 27 (c) 54 (d) 81

**66.** What is *f*(1) *s f*(4) equal to?

(a) 4 (b) 8 (c) 9 (d) 18 **Direction for Questions (67-68):** Consider the following for the two (02) items that follow: A function *f* is such that f(xy) = f(x + y) for all real values of *x* and *y* and f(5) = 10

- **67.** What is f(0) equal to?
  - (a) 0 (b) 1 (c) 5 (d) 10
- **68.** What if f(20) + f(-20) equal to? **(a)** 0 **(b)** 10 **(c)** 20 **(d)** 40 **Direction for Questions (69-70):** Consider the following for the two (02) items that follow: Let  $f(x) = [x^2]$ , where [,] is the greater integer function.

**69.** What is 
$$\int_{\sqrt{2}}^{\sqrt{3}} f(x)$$
 equal to?

(a) 
$$\sqrt{3} - \sqrt{2}$$
 (b)  $2(\sqrt{3} - \sqrt{2})$   
(c)  $3 - \sqrt{2}$  (d) 1

70. What is  $\int_{\sqrt{2}}^{2} f(x) dx$  equal to?

(a) 
$$6 - \sqrt{3} - 2\sqrt{2}$$
 (b)  $6 - \sqrt{3} - \sqrt{2}$   
(c)  $6 - \sqrt{3} + 2\sqrt{2}$  (d)  $6 + \sqrt{3} - 2\sqrt{2}$ 

**71.** If  $A^2 + B^2 + C^2 = 0$ , then what is the value of the following?

**72.** If  $\omega$  is a non-real cube root of unity, then what is a root of the following equation?

$$\begin{vmatrix} x+1 & \omega & \omega^2 \\ \omega & x+\omega^2 & 1 \\ \omega^2 & 1 & x+\omega \end{vmatrix} = 0$$
(a)  $x = 0$  (b)  $x = 1$   
(c)  $x = \omega$  (d)  $x = \omega^2$ 

**73.** What is  $\left(\frac{\sqrt{3}+i}{\sqrt{3}-i}\right)^3$  equal to?

(a) 
$$-1$$
 (b) 0 (c) 1 (d) 3

74. If 
$$x^2 - x + 1 = 0$$
, then what is  
 $\left(x - \frac{1}{x}\right)^2 + \left(x - \frac{1}{x}\right)^4 + \left(x - \frac{1}{x}\right)^8$  is equal to?  
(a) 81 (b) 85 (c) 87 (d) 90

75. How many 7-letter words (with or without meaning) can be constructed using all the letters of the word CAPITAL so that all consonants come together in each word?
(a) 360 (b) 300 (c) 288 (d) 240

- **76.** If  $z \neq 0$  is a complex number, then what is  $amp(z) + amp(\overline{z})$  equal to?
  - (a) 0 (b)  $\frac{\pi}{2}$ (c) π (d) 2π
- 77. How many sides are there in a polygon which has 20 diagonals?

**(b)**7 (c) 8 (d) 10 (a) 6

- 78. In how many ways can the letters of the word DELHI be arranged keeping the positions of vowels and consonants unchanged? (d) 24 (a) 6 **(b)** 9 (c) 12
- 79. What is the number of positive integer solutions of x + y + z = 5?

(a) 
$$3$$
 (b)  $5$  (c)  $6$  (d)  $9$ 

80. What is the number of rational terms in the expansion of  $(3^{1/2} + 5^{1/4})^{12}$ ?

(a) 
$$2$$
 (b)  $3$  (c)  $4$  (d)  $6$ 

- **81.** Under what condition will the lines  $m^2 x + ny 1$ = 0 and  $n^2x - my + 2 = 0$  be perpendicular? (a) mn - 1 = 0**(b)** mn + 1 = 0
  - (c) m + n = 0(d) m - n = 0
- **82.** If p and q are real numbers between 0 and 1 such that the points (p, 1), (1, q) and (0, 0) form an equilateral triangle, then what is (p + q) equal to?
  - (a)  $\sqrt{2}$ **(b)**  $\sqrt{2} - 1$
  - (c)  $2-\sqrt{3}$ (d)  $4 - 2\sqrt{3}$
- **83.** The vertices of a triangle are A(1, 1), B(0, 0) and C(2, 0). The angular bisectors of the triangle meet at *P*. What are the coordinates of *P*?
  - (a)  $(1,\sqrt{2}-1)$ **(b)**  $(1,\sqrt{3}-1)$ (c)  $\left(1,\frac{1}{2}\right)$  (d)  $\left(\frac{1}{2},\sqrt{2}-1\right)$
- **84.** Let A(3, -1)j and B(1, 1) be the end points of line segment AB. Let P be the middle point of the line segment AB. Let Q be the point situated at a distance of  $\sqrt{2}$  units from P on the perpendicular bisector line of AB. What are the possible coordinates of Q?

(a) 
$$(2, 1)$$
 (b)  $(3, 1)$  (c)  $(2, 2)$  (d)  $(1, 3)$ 

85. ABC is an equilateral triangle and AD is the altitude on BC. If the coordinates of A are (1, 2) and that of D are (-2, 6) then what is the equation of *BC*?

(a) 3x + 4y - 18 = 0 (b) 4x + 3y - 1 = 0(c) 4x - 3y = 26(d) 3x - 4y + 30 = 0

- 86. What is the equation of the circle whose diameter is 10 cm and the equation of two of its diameters are x + y = 0 and x - y = 0? (a)  $x^2 + y^2 = 0$ (b)  $x^2 + y^2 = 25$ (c)  $x^{2} + y^{2} = 100$ (d)  $x^{2} + y^{2} - 2x - 2y - 23 = 0$
- 87. A square is inscribed in a circle  $x^2 + y^2 + 2x + 2y$ + 1 = 0 and its sides are parallel to coordinate axes. Which one of the following is a vertex of the square?

(a) 
$$(-2, 2)$$
  
(b)  $(-2, -2)$   
(c)  $\left(-1 + \frac{1}{\sqrt{2}}, -1 - \frac{1}{\sqrt{2}}\right)$ 

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(d) None of the above

- **88.** A tangent to the parabola  $y^2 = 4x$  is inclined at an angle of 45° with the positive direction of x-axis. What is point of contact of the tangent and the parabola?
  - (b)  $(2,\sqrt{2})$ (a) (1, 1) (d) (1, 2) (c)  $\left(\frac{1}{2}, \frac{1}{\sqrt{2}}\right)$
- 89. What is the distance between the two foci of the hyperbola  $25x^2 - 75y^2 = 225$ ?
  - (a)  $2\sqrt{3}$  units (b)  $4\sqrt{3}$  units (c)  $\sqrt{6}$  units (d)  $2\sqrt{6}$  units
- **90.** If any point on an ellipse is  $(3\sin\alpha, 5\cos\alpha)$ , then what is the eccentricity of the ellipse?

(a) 
$$\frac{4}{3}$$
 (b)  $\frac{4}{5}$  (c)  $\frac{3}{4}$  (d)  $\frac{1}{2}$ 

Direction for Questions (91-94): Consider the following for the four (04) times that follow: The frequency distribution of height of students of a class is given below:

Height (in cm)	Number of students
160–162	12
162–164	15
164–166	24
166–168	13

91. What is the total number of students whose height is less than or equal to 165 cm?

(a) 15	(b)	39
(c) 51	(d)	Nor

(d) None of the above

- 92. What is the median height of the class? (a) 162.41 cm (b) 163.41 cm
  - (c) 164.41 cm (d) 165.41 cm

**93.** The height which occurs most frequently in the class is:

(a) 16	63.5 cm	(b)	163.9 cm
(c) 16	64.5 cm	(d)	164.9 cm

- **94.** The most appropriate graphical representation of the given frequency distribution is:
  - (a) bar chart
  - (b) percentage bar chart
  - (c) histogram
  - (d) pie chart

**Direction for Questions (95-96):** Consider the following for the two (02) items that follow:

The sum and the sum of squares of the observation corresponding to length *X* (in cm) and weight *Y* (in gm) of 50 tropical tubers are given as  $\Sigma X = 200$ ,  $\Sigma Y = 250$ ,  $\Sigma X^2 = 900$  and  $\Sigma Y^2 = 1400$ .

- 95. Which of the following is correct?
  - (a) Variance (X) > Variance (Y)
  - **(b)** Variance (X) < Variance (Y)
  - (c) Variance (X) = Variance (Y)
  - (d) Cannot be determined from the given data
- **96.** Which one of the following statements is correct?
  - (a) Coefficient of variation of *X* is strictly more than coefficient of variation of *Y*.
  - (b) Coefficient of variation of X is strictly less than coefficient of variation of Y.
  - (c) Coefficient of variation of X is the same as coefficient of variation of Y.
  - (d) Coeficient of variation cannot be determined from the given data.

**Direction for Questions (97-98):** Consider the following for the two (02) items that follow: Let X be a random variable following binomial distribution with parameters n = 6 and p = k. Further, 9P(X = 4) = P(X = 2).

**97.** What is the value of *k*?

(a) 
$$\frac{1}{2}$$
 (b)  $\frac{1}{3}$  (c)  $\frac{1}{4}$  (d)  $\frac{1}{5}$ 

**98.** What is the value of P(X = 3)?

(a)	$\frac{135}{1024}$	(b)	$\frac{5}{128}$
(c)	$\frac{45}{1024}$	(d)	$\frac{70}{1024}$

**Direction for Questions (99-100):** Consider the following for the two (02) items that follow: A committee of 6 members is formed from a group of 7 gentlemen and 4 ladies.

**99.** What is the probability that the committee includes exactly 3 gentlemen?

(a) 
$$\frac{10}{33}$$
 (b)  $\frac{30}{77}$  (c)  $\frac{100}{231}$  (d)  $\frac{5}{11}$ 

**100.** What is the probability that the committee includes at least 2 ladies?

(a) 
$$\frac{41}{66}$$
 (b)  $\frac{47}{66}$  (c)  $\frac{49}{66}$  (d)  $\frac{53}{66}$ 

**Direction for Questions (101-102):** Consider the following for the two (02) items that follow: Let the function  $y = (1 - \cos x)^{-1}$ , where  $x \neq 2n\pi$  and *n* is an integer.

**101.** What is the range of the function?

(a) [0, ∞)	(b)	(0.5 <i>,</i> ∞)
(c) [1,∞)	(d)	(-∞, 0.5]

**102.** What is  $\int y dx$  equal to?

(a) 
$$-\tan\left(\frac{x}{2}\right) + c$$
 (b)  $-\cot\left(\frac{x}{2}\right) + c$   
(c)  $\tan\left(\frac{x}{2}\right) + c$  (d)  $\cot\left(\frac{x}{2}\right) + c$ 

where *c* is the constant of integration. **Direction for Questions (103-104):** Consider the following for the two (02) items that follow: Let the function f(x) = sin[x], where [.] is the greatest integer function and g(x) = [x].

**103.** What is  $\lim \{f(x)g(x)\}$  equal to?

- **104.** What is  $\lim_{x\to 0} \frac{f(x)}{g(x)}$  equal to?
  - (a)  $-\sin 1$  (b)  $\sin 1$ (c) 0 (d) Limit does not exist **Direction for Questions (105-106):** Consider the following for the two (02) items that follow: Let the curve f(x) = |x-3|.
- **105.** What is the domain of the function f(x)?
  - (a)  $(0, \infty)$  (b)  $(3, \infty)$ (c)  $(-\infty, \infty)$  (d)  $(-\infty, \infty) - \{3\}$
- **106.** What is the area bounded by the curved f(x) and y = 3?
  - (a) 3 square units (b) 4.5 square units (c) 7.5 square units (d) 9 square units **Direction for Questions (107-108):** Consider the following for the two (02) items that follow: Let  $f = \{(1, 1), (2, 4), (3, 7), (4, 10)\}$
- **107.** If f(x) = px + q, then what is the value of (p + q)? (a) -1 (b) 0 (c) 1 (d) 5

- 108. Consider the following statements:
  - I. *f* is an one-one function.
  - II. *f* is onto function if the codomain is the set of natural numbers.

Which of the statements given above is/are correct?

(a) I only (b) II only

(c) Both I and II (d) Neither I nor II Direction for Questions (109-110): Consider the following for the two (02) items that follow: Let the function  $f(x) = x^2 - 1$ .

**109.** What is 
$$\lim_{x \to 1} {f.f((x))}$$
 equal to?  
**(a)** -1 **(b)** 0 **(c)** 1 **(d)** 2

- **110.** What is the area bounded by the function *f*(*x*) and the *x*-axis?
  - (a)  $\frac{1}{3}$  square units (b)  $\frac{2}{3}$  square unit (c)  $\frac{4}{2}$  square units (d) 2 square units

**Direction for Questions (111-112):** Consider the following for the two (02) items that follow: Let  $x = \sec\theta - \cos\theta$  and  $y = \sec^4\theta - \cos^4\theta$ ,

**111.** What is 
$$\left(\frac{dy}{dx}\right)^2$$
 equal to?  
**(a)**  $\frac{4(y^2 + 4)}{(x^2 + 4)}$  **(b)**  $\frac{4(y^2 - 4)}{(x^2 - 4)}$   
**(c)**  $\frac{16(y^2 + 4)}{(x^2 + 4)}$  **(d)**  $\frac{16(y^2 - 4)}{(x^2 - 4)}$ 

**112.** What is 
$$\left(\frac{x^2+4}{y^2+4}\right)\frac{dy}{dx}\left[(x^2+4)\frac{d^2y}{dx^2}-16y\right]$$
 equal to?

(a) 16x (b) 16y (c) -16x (d) -16yDirection for Questions (113-114): Consider the following for the two (02) items that follow: Let *ABC* be a triangle right-angled at *B* and *AB* + *AC* = 3 units.

**113.** What is  $\angle A$  equal to if the area of the triangle is maximum?

(a)  $\frac{\pi}{6}$  (b)  $\frac{\pi}{4}$  (c)  $\frac{\pi}{3}$  (d)  $\frac{5\pi}{12}$ 

- 114. What is the maximum area of the triangle?
  - (a)  $\frac{\sqrt{3}}{2}$  square unit (b)  $\sqrt{3}$  square unit
  - (c)  $\frac{\sqrt{6}}{2}$  square unit (d)  $\sqrt{6}$  square unit

**Direction for Questions (115-116):** Consider the following for the two (02) items that follow: Let  $(x + y)^{p + q} = x^p y^p$ , where *p*, *q* are positive integers.

**115.** The derivative of *y* with respect to *x*:

- (a) depends on *p* only
- (b) depends on *q* only
- (c) depends on both *p* and *q*
- (d) is independent of both *p* and *q*

**116.** If 
$$p + q = 10$$
, then what is  $\frac{dy}{dx}$  equal to?

(a) 
$$\frac{y}{x}$$
 (b)  $xy$   
(c)  $x^{10}y^{10}$  (d)  $\left(\frac{y}{x}\right)^{10}$ 

**Direction for Questions (117-118):** Consider the following for the two (02) items that follow: The slope of the tangent of the curve y = f(x) at (x, f(x)) is 4 for every real number x and the curve passes through the origin.

- **117.** What is the nature of the curve?
  - (a) A straight line passing through (1, 4)
  - **(b)** A straight line passing through (-1, 4)
  - (c) A parabola with vertex at origin and focus at (2, 0)
  - (d) A parabola with vertex at origin and focus at (1, 0)
- **118.** What is the area bounded by the curve the x-axis and the line x = 4?
  - (a) 8 square units (b) 16 square units

(c) 32 square units (d) 64 square units **Direction for Questions (119-120):** Consider the following for the two (02) items that follow:

Let 
$$f(x) = \begin{cases} x^3, & x^2 < 1 \\ x^2, & x^2 \ge 1 \end{cases}$$

**119.** What is  $\lim_{x\to 0} f'(x)$  equal to?

(a) 2
(b) 1
(c) 0
(d) Limit does not exist

**120.** Consider the following statements:

- I. The function is continuous at x = -1
- II. The function is differentiable at x = 1
- (a) I only
- (b) II only
- (c) Both I and II
- (d) Neither I nor II

Answer Key			
Q. No	Answer Key	Chapter's Name	Topic's Name
1	с	Binomial Theorem	Expansion
2	b	Algebra	Linear inequality
3	d	Matrices	Multiplication of matrices
4	b	Matrices	Orthogonal Matrices
5	c	Determinants	Properties
6	d	Matrices	Multiplication of matrices
7	d	Matrices	Multiplication of matrices
8	b	Permutation ans Combination	Combinations
9	d	Permutation ans Combination	Combinations
10	b	Matrices	Orthogonal Matrices
11	с	Trigonometry	General
12	d	Trigonometry	General
13	с	Trigonometry	General
14	с	Trigonometry	Special angles
15	b	Trigonometry	Special angles
16	b	Triangle	Angles of triangle
17	c	Triangle	Properties
18	a	Trigonometry	Applications of Trigonometry
19	d	Quadratic Equations	Roots of equation
20	с	Inverse Trigonometry	Properties
21	b	Three Dimensional Geometry	Direction cosines
22	с	Coordinate Geometry	Area
23	d	Coordinate Geometry	Area
24	а	Three Dimensional Geometry	Direction cosines
25	b	Three Dimensional Geometry	Equation of Plane
26	d	Vectors	Dot product
27	c	Vectors	Coplanar vectors
28	b	Vectors	Position Vectors
29	a	Vectors	Triple product
30	a	Vectors	Unit Vectors
31	b	Sequence and Series	Arithmetic Progression
32	b	Sequence and Series	Geometric Progression
33	b	Quadratic Equations	Roots of equation
34	a	Algebra	Linear Equations in Two Variables
35	a	Sequence and Series	AP, GP
36	с	Sequence and Series	AP, GP, HP

Q. No	Answer Key	Chapter's Name	Topic's Name
37	d	Algebra	Modulo
38	а	Determinants	Cofactors
39	а	Determinants	Properties
40	b	Determinants	Expansion
41	b	Trigonometry	Properties
42	а	Trigonometry	Properties
43	с	Trigonometry	Properties
44	а	Trigonometry	Minimum Value
45	b	Trigonometry	Maximum Value
46	с	Triangle	Properties
47	с	Triangle	Ang <mark>les of t</mark> riangle
48	а	Triangle	Area
49	b	Trigonometry	Applications of Trigonometry
50	а	Trigonometry	Applications of Trigonometry
51	с	Statistics and Probability	Probability
52	b	Statistics and Probability	Probability
53	а	Statistics and Probability	Mean
54	b	Statistics and Probability	Standard Deviation
55	b	Statistics and Probability	Conditional Probability
56	b	Statistics and Probability	Probability
57	b	Statistics and Probability	Probability
58	с	Statistics and Probability	Binomial Distribution
59	b	Statistics and Probability	Binomial Distribution
60	с	Statistics and Probability	Mean
61	d	Trigonometry	Inverse Trigonometry
62	с	Trigonometry	Derivatives
63	с	Calculus	Limits
64	d	Calculus	Maxima/ Minima
65	d	Function	Value of functtion
66	с	Function	Value of functtion
67	d	Function	Value of functtion
68	с	Function	Value of functtion
69	b	Integral Calculus	Definite integration
70	a	Integral Calculus	Definite integration
71	b	Determinants	Expansion
72	a	Determinants	Expansion
73	а	Complex Numbers	Expansion

Q. No	Answer Key	Chapter's Name	Topic's Name
74	с	Quadratic Equations	Roots of equation
75	с	Permutation ans Combination	Combinations
76	а	Complex Numbers	Amplitude
77	с	Permutation ans Combination	Combinations
78	с	Permutation ans Combination	Combinations
79	с	Permutation ans Combination	Combinations
80	с	Binomial Theorem	Expansion
81	а	Algebra	Linear Equations in Two Variables
82	d	Calculus	Distance Formula
83	а	Calculus	Distance Formula
84	b	Calculus	Equation of Line
85	d	Calculus	Equation of Line
86	b	Calculus	Equation of Circle
87	с	Calculus	Distance Formula
88	d	Parabola	Tangent
89	b	Hyyperbola	Focii
90	а	Ellipse	Eccentricity
91	с	Statistics and Probability	Frequency
92	с	Statistics and Probability	Median
93	d	Statistics and Probability	Mode
94	с	Statistics and Probability	Frequency polygon
95	b	Statistics and Probability	Variance
96	b	Statistics and Probability	Coefficient of Variation
97	с	Statistics and Probability	Binomial Distribution
98	а	Statistics and Probability	Binomial Distribution
99	а	Statistics and Probability	Probability
100	d	Statistics and Probability	Probability
101	b	Function	Range
102	b	Function	Indefinite integral
103	b	Function	Limits
104	d	Function	Limits
105	с	Function	Domain
106	d	Function	Area under the Curve
107	с	Function	Value of Function
108	а	Function	One one, Onto Function
109	а	Function	Limits

Q. No	Answer Key	Chapter's Name	Topic's Name
110	С	Function	Area under the Curve
111	с	Calculus	Derivatives
112	с	Calculus	Derivatives
113	с	Calculus	Maxima/ Minima
114	а	Calculus	Maxima/ Minima
115	d	Calculus	Derivatives
116	а	Calculus	Derivatives
117	а	Calculus	Slope
118	с	Calculus	Area under the Curve
119	с	Function	Limits
120	d	Calculus	Continuity and Differentiability

### NDA/NA National Defence Academy /

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MATHEMATICS

SOLVED PAPER

 $\begin{bmatrix} 1 & 0 & 0 \end{bmatrix}$ 

#### **ANSWERS WITH EXPLANATIONS**

**Option (c) is correct.** 1. *Explanation:* Put x = 1 and y = 1, we get Sum of coefficients =  $2^n = 256$ Total terms = 8 + 1 = 9Greatest term = middle term =  $\frac{9+1}{2}$  $= 5^{th} term$ 2. Option (b) is correct. *Explanation:*  $k < (\sqrt{2} + 1)^3 < k + 2$  $\Rightarrow k < 2\sqrt{2} + 1 + 6 + 3\sqrt{2} < k + 2$  $\rightarrow k < 5\sqrt{2} + 7 < k + 2$  $\Rightarrow k < 14.07 < k + 2$  $\Rightarrow$  *k* < 14.07 and *k* > 12.07 k = 13, 14*.*.. 3. Option (d) is correct. Explanation:  $\begin{bmatrix} x & 1 & 1 \end{bmatrix} \begin{bmatrix} 1 & 2 & 3 \\ 4 & 5 & 6 \\ 7 & 8 & 9 \end{bmatrix} \begin{bmatrix} 1 \\ 1 \\ x \end{bmatrix} = [45]$  $\Rightarrow [x + 11 + 2x + 13 + 3x + 15] \begin{bmatrix} 1 \end{bmatrix}$ 1 = [45] x  $\Rightarrow x + 11 + 2x + 13 + 3x^{2} + 15x = 45$  $3x^{2} + 18x + 24 = 45$  $x^{2} + 6x - 7 = 0$  $\Rightarrow$  $\Rightarrow$ x = -7 and 1  $\rightarrow$ 4. Option (b) is correct. Explanation: For orthogonal matrix.  $A^{T} = A^{-1} \Rightarrow AA^{T} = I$  $A^2 = I(:: A \text{ is symmetric})$  $\begin{bmatrix} y & z & x \\ z & x & y \\ x & y & z \end{bmatrix} \begin{bmatrix} y & z & x \\ z & x & y \\ x & y & z \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}$  $y^2 + z^2 + x^2$  yz + zx + xy xy + yz + xzyz + zx + xy  $x^2 + y^2 + z^2$  xy + yz + zx $xy + yz + zx \quad xy + yz + zx \quad x^2 + y^2 + z^2$ 

 $= \begin{bmatrix} 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}$ x<sup>2</sup> + y<sup>2</sup> + z<sup>2</sup> = 1 5. Option (c) is correct.

*Explanation:* For non-singular matrix we know that

$$|\mathbf{M}^{n}| = |\mathbf{M}|^{n}, |\mathbf{M}^{-1}| = \frac{1}{|\mathbf{M}|}$$

and  $|\mathbf{M}^{\mathrm{T}}| = |\mathbf{M}|$ 

6. Option (d) is correct. *Explanation:* 

$$f(\pi) = \begin{bmatrix} \cos \pi & \sin \pi \\ -\sin \pi & \cos \pi \end{bmatrix} = \begin{bmatrix} -1 & 0 \\ 0 & -1 \end{bmatrix}$$
$$[f(\pi)]^2 = \begin{bmatrix} -1 & 0 \\ 0 & -1 \end{bmatrix} \begin{bmatrix} -1 & 0 \\ 0 & -1 \end{bmatrix} = \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$$

. Option (d) is correct. *Explanation:* 

$$A^{2} = \begin{bmatrix} 1 & 2 & 2 \\ 2 & 1 & 2 \\ 2 & 2 & 1 \end{bmatrix} \begin{bmatrix} 1 & 2 & 2 \\ 2 & 1 & 2 \\ 2 & 2 & 1 \end{bmatrix} \begin{bmatrix} 1 & 2 & 2 \\ 2 & 1 & 2 \\ 2 & 2 & 1 \end{bmatrix} = \begin{bmatrix} 9 & 8 & 8 \\ 8 & 9 & 8 \\ 8 & 8 & 9 \end{bmatrix}$$
$$A^{2} - 4A = \begin{bmatrix} 9 & 8 & 8 \\ 8 & 9 & 8 \\ 8 & 9 & 8 \\ 8 & 8 & 9 \end{bmatrix} - \begin{bmatrix} 4 & 8 & 8 \\ 8 & 4 & 8 \\ 8 & 8 & 4 \end{bmatrix} = \begin{bmatrix} 5 & 0 & 0 \\ 0 & 5 & 0 \\ 0 & 0 & 5 \end{bmatrix}$$
$$= 5I_{3}$$

8. Option (b) is correct.  
Explanation: 
$${}^{5n}C_r = {}^{5n}C_{n+r}$$
  
 $n+r+r = 5n \Rightarrow 2r = 4n \Rightarrow r = 2n$ 

- 9. Option (d) is correct. *Explanation:* Number of selections (at most 3 things)
  - $= {}^{6}C_{0} + {}^{6}C_{1} + {}^{6}C_{2} + {}^{6}C_{3}$  $= 1 + 6 + \frac{6 \cdot 5}{2 \cdot 1} + \frac{6 \cdot 5 \cdot 4}{3 \cdot 2 \cdot 1}$ = 1 + 6 + 15 + 20 = 42

10. Option (b) is correct.

*Explanation:* We know that for orthogonal matrix

- $\begin{array}{l} \mathbf{A}^{\mathrm{T}} &= \mathbf{A}^{-1} \Longrightarrow \mathbf{A} \mathbf{A}^{\mathrm{T}} = \mathbf{A} \mathbf{A}^{-1} = \mathbf{I} \\ \mathbf{A}^{2} &= \mathbf{I} \ (\because \ \mathbf{A} = \mathbf{A}^{\mathrm{T}}) \end{array}$
- 11. Option (c) is correct.

Explanation:

 $\frac{p}{q} = \frac{\tan 2\alpha - \tan \alpha}{\cot \alpha - \cot 2\alpha} = \frac{\tan 2\alpha - \tan \alpha}{\frac{1}{\tan \alpha} - \frac{1}{\tan 2\alpha}}$  $= \frac{(\tan 2\alpha - \tan \alpha)\tan \alpha \cdot \tan 2\alpha}{(\tan 2\alpha - \tan \alpha)}$ 

$$=$$
 tan $\alpha$  . tan $2\alpha$ 

#### 12. Option (d) is correct.

*Explanation:*  $p + q = \tan 2\alpha - \tan \alpha + \cot \alpha$ -  $\cot 2\alpha$ 

$$= \left(\frac{\sin^2 2\alpha - \cos^2 2\alpha}{\sin 2\alpha \cdot \cos 2\alpha}\right) + \left(\frac{\cos^2 \alpha - \sin^2 \alpha}{\sin \alpha \cdot \cos \alpha}\right)$$
$$= \frac{\sin^2 2\alpha - \cos^2 2\alpha}{\sin 2\alpha \cdot \cos 2\alpha} + \frac{\cos^2 \alpha - \sin^2 \alpha}{\sin \alpha \cdot \cos \alpha}$$
$$= \frac{-2\cos 4\alpha}{\sin 4\alpha} + \frac{2\cos 2\alpha}{\sin 2\alpha}$$

$$= \frac{2(\sin 4\alpha \cdot \cos 2\alpha - \cos 4\alpha \cdot \sin 2\alpha)}{\sin 4\alpha \cdot \sin 2\alpha}$$

$$= \frac{2\sin(4\alpha - 2\alpha)}{\sin 4\alpha \cdot \sin 2\alpha} = \frac{2 \cdot \sin 2\alpha}{\sin 4\alpha \cdot \sin 2\alpha}$$

=  $2 \operatorname{cosec} 4\alpha$ .

13. Option (c) is correct.

Explanation: 
$$\frac{p}{p+2q} = \frac{1}{1+\frac{2q}{p}} = \frac{1}{1+\frac{2}{\tan \alpha \cdot \tan 2\alpha}}$$

 $= \frac{\sin \alpha \cdot \sin 2\alpha}{\sin \alpha \cdot \sin 2\alpha + \cos \alpha \cdot \cos 2\alpha + \cos \alpha \cdot \cos 2\alpha}$ 

$$= \frac{\sin \alpha \cdot \sin 2\alpha}{\cos \alpha + \cos \alpha \cdot \cos 2\alpha} = \frac{\sin \alpha \cdot 2 \sin \alpha \cdot \cos \alpha}{\cos \alpha \cdot 2 \cdot \cos^2 \alpha}$$
$$= \tan^2 \alpha.$$

14. Option (c) is correct. Explanation:  $\cos \alpha = 2(1 - \sin \alpha)$ 

$$\Rightarrow \frac{\cos^2 \alpha}{(1 - \sin \alpha)^2} = 4$$
$$\frac{1 + \sin \alpha}{1 - \sin \alpha} = \frac{4}{1} \Rightarrow \sin \alpha = \frac{3}{5}$$
$$\tan \alpha = \frac{3}{\sqrt{25 - 9}} = \frac{3}{4}$$

15. Option (b) is correct. Explanation:  $\therefore \sin \alpha = \frac{3}{5}$  and  $\cos \alpha = \frac{4}{5}$   $\therefore 2\sin 2\alpha + \cos 2\alpha = 4\sin \alpha$ .  $\cos \alpha + 1 - 2\sin^2 \alpha$   $= \frac{48}{25} + 1 - \frac{18}{25} = \frac{48 + 25 - 18}{25} = \frac{55}{25} = \frac{11}{5}$ 16. Option (b) is correct. Explanation: A a a a b a a c  $\frac{a}{\sin 3x} = \frac{b}{\sin x}$   $\Rightarrow \frac{a}{b} = \frac{\sin 3x}{\sin x}$  $\Rightarrow 2 = \frac{\sin 3x}{\sin x} \Rightarrow 2\sin x = 3\sin x - 4\sin^3 x$ 

$$\Rightarrow \sin x = 0 \Rightarrow \sin x = \frac{1}{2}$$

$$\Rightarrow x = 30^{\circ}$$

17. Option (c) is correct.

**Explanation:**  $\angle B = x = 30^\circ$ ,  $\angle A = 3x = 90^\circ$ ,  $\angle C = 180^\circ - 120^\circ = 60^\circ$  $\therefore$  Triangle is right-angled.  $\therefore 30^\circ$ , 60° and 90° are in A.P.

So options (I) and (III) are only correct.

**18.** Option (a) is correct. *Explanation:* 



19. Option (d) is correct. Explanation:  $\therefore x^2 - 4x + 1 = 0$  $\Rightarrow x = 2 \pm \sqrt{3} > 0$ 

$$\therefore \tan^{-1} k + \tan^{-1} \frac{1}{k} = \tan^{-1} \left( \frac{k + \frac{1}{k}}{1 - k \times \frac{1}{k}} \right)$$
$$\tan^{-1} \infty = \frac{\pi}{2}$$

20. Option (c) is correct.

*Explanation:*  $\tan^{-1}k + \tan^{-1}\frac{1}{2} = \frac{\pi}{4} = \tan^{-1}1$ 

$$\tan^{-1}k = \tan^{-1}\left(\frac{1-\frac{1}{2}}{1+\frac{1}{2}}\right) = \tan^{-1}\left(\frac{1}{2} \times \frac{2}{3}\right)$$
$$k = \frac{1}{3}$$

21. Option (b) is correct. *Explanation:* We know that  $\cos^2 \alpha + \cos^2 \beta + \cos^2 \gamma = 1$  ...(i) and  $\cos(\alpha + \beta) \cos(\alpha - \beta) = \cos^2 \alpha - \sin^2 \beta$  $= \cos^2 \alpha + \cos^2 \beta - 1 = 1 - \cos^2 \gamma - 1 = -\cos^2 \gamma$ .

22. Option (c) is correct.  
Explanation:  
Area = AB × BC  
= 
$$\sqrt{1^2 + 3^2 + 1^2} \times \sqrt{2^2 + 1^2 + 1^2}$$
  
=  $\sqrt{11} \times \sqrt{6}$   
=  $\sqrt{66}$  sq. units

- **23.** Option (d) is correct. *Explanation:* D.rs of AB = *k*, -1, 3 D.rs of BC = 2, *k*, -1
  - $\therefore AB \perp BC$
  - $\therefore \qquad 2k k 3 = 0 \Rightarrow k = 3$
- **24.** Option (a) is correct. *Explanation:* D.rs of line are *p*, *q*, *r*

where 
$$p = 2q = 3r \Rightarrow \frac{p}{6} = \frac{q}{3} = \frac{r}{2}$$
  
 $\therefore$  D.rs of line are 6, 3, 2

$$\cos \theta = \frac{18}{\sqrt{6^2 + 3^2 + 2^2}} = \frac{18}{7}$$

$$\cos 2\theta = 2\cos^2\theta - 1 = \frac{10}{49} - 1 = \frac{10}{49}$$

3

-31

#### 25. Option (b) is correct.

*:*.

*Explanation:* Point (1, 1, 1) and d.rs of normal are <3, 2, 1>

$$\therefore \text{ Equation of the plane is} 3(x-1) + 2(y-1) + 1(z-1) = 0 \Rightarrow 3x + 2y + z = 6$$

26. Option (d) is correct. Explanation:  $\because \cos^2 \alpha + \cos^2 \beta + \cos^2 \gamma = 1$   $\Rightarrow \sin^2 \alpha + \sin^2 \beta + \sin^2 \gamma = 2$ Now,  $\vec{a}.\vec{b}. = \sin^2 \alpha + \sin^2 \beta + \sin^2 \gamma = 2$ 27. Option (c) is correct. Explanation:  $\vec{d} = (\vec{a} \times \vec{b}) \times \vec{c} = (\vec{a}.\vec{c})\vec{b} - (\vec{b}.\vec{c})\vec{a}$  ...(i) Since  $\vec{d}$  is a linear combination of  $\vec{a}$  and  $\vec{b}$ . Therefore  $\vec{d}$  lies in the plane formed by  $\vec{a}$  and  $\vec{b}$ . So,  $\vec{d}$  is coplanar with  $\vec{a}$  and  $\vec{b}$ .  $\vec{d}.\vec{c} = \left[(\vec{a}.\vec{c})\vec{b} - (\vec{b}.\vec{c})\vec{a}\right].\vec{c}$ 

$$= (\vec{a}.\vec{c})(\vec{b}.\vec{c}) - (\vec{b}.\vec{c})(\vec{a}.\vec{c}) = 0$$

So,  $\vec{d}$  is perpendicular to  $\vec{c}$ Hence both statements are true.

#### 28. Option (b) is correct.

Explanation: 
$$\because 3\vec{a} - 4\vec{b} + \vec{c} = 0$$
  
 $\Rightarrow 3\vec{a} - 3\vec{b} - \vec{b} + \vec{c} = 0$   
 $\Rightarrow 3(\vec{a} - \vec{b}) = \vec{b} - \vec{c} \Rightarrow 3(\vec{b} - \vec{a}) = \vec{c} - \vec{b}$   
 $\Rightarrow \frac{\vec{b} - \vec{a}}{\vec{c} - \vec{b}} = \frac{1}{2} \Rightarrow \frac{\overline{AB}}{\overline{BC}} = \frac{1}{3}$ 

#### 29. Option (a) is correct.

**Explanation:**  $(\vec{a} \times \vec{b}) + (\vec{b} \times \vec{c}) + (\vec{c} \times \vec{a})$ 

 $= (\vec{a} \times \vec{b}) + (\vec{b} \times \vec{a}) \times \vec{c}$   $= (\vec{a} \times \vec{b}) + (\vec{b} \times \vec{a}) \times (\cos^2 \theta \vec{a} + \sin^2 \theta \vec{b})$   $= (\vec{a} \times \vec{b}) + \cos^2 \theta (\vec{b} \times \vec{a}) - \sin^2 \theta (\vec{a} \times \vec{b})$   $= (\vec{a} \times \vec{b}) - \cos^2 \theta (\vec{a} \times \vec{b}) - \sin^2 \theta (\vec{a} \times \vec{b})$  $= (\vec{a} \times \vec{b}) [1 - (\cos^2 \theta + \sin^2 \theta)] = 0$ 

#### 30. Option (a) is correct.

Explanation: 
$$|a| = |b| = |a \times b| = 1$$
  
 $\sin \theta = \frac{|\vec{a} \times \vec{b}|}{|\vec{a}| |\vec{b}|} = 1.$   
 $\therefore \qquad \theta = \frac{\pi}{2}$ 

Now,  $\vec{a}.\vec{b} = |\vec{a}| |\vec{b}| \cos{\frac{\pi}{2}} = 0$ 

31. Option (b) is correct. Explanation:  $S_k = 3k^2 + 5k$   $S_1 = 3 + 5 = 8$   $S_2 = 12 + 10 = 22$   $S_3 = 27 + 15 = 42$   $a_1 = S_1 = 8$  $a_2 = S_2 - S_1 = 22 - 8 = 14$   $a_3 = S_3 - S_2 = 42 - 22 = 20$   $\therefore$  Series = 8 + 14 + 20 ..... are in A.P. with common difference = 14 - 8 = 6.

- 32. Option (b) is correct. Explanation:  $S_8 = 5S_4$   $\frac{a(r^8 - 1)}{r - 1} = \frac{5 \cdot a(r^4 - 1)}{r - 1}$   $\Rightarrow \qquad \frac{r^8 - 1}{r^4 - 1} = 5 \Rightarrow \frac{(r^4 - 1)(r^4 + 1)}{r^4 - 1} = 5$  $\Rightarrow \qquad r^4 = 4 \Rightarrow r = \pm\sqrt{2}, \pm\sqrt{2}i$
- 33. Option (b) is correct. Explanation: Here,  $\alpha + \beta = k$ ,  $\alpha\beta = k$ and  $\alpha - \beta = (2\sqrt{3})$   $\therefore \qquad (\alpha - \beta)^2 = (\alpha + \beta)^2 - 4\alpha\beta$   $\Rightarrow \qquad (2\sqrt{3})^2 = k^2 - 4k$   $\Rightarrow \qquad k^2 - 4k - 12 = 0 \Rightarrow k^2 - 6k + 2k - 12 = 0$  $\Rightarrow \qquad (k - 6) (k + 2) = 0 \Rightarrow k = -2, 6$
- 34. Option (a) is correct. *Explanation:*

$$xy + 5 = 4y$$

$$xy + 5 = -4x$$

$$- - +$$

$$0 = 4(x + y)$$

$$x + y = 0$$

35. Option (a) is correct. *Explanation:* 

 $\Rightarrow$ 

 $a_{5} = a + 4d, a_{7} = a + 6d \text{ and } a_{13} = a + 12d$  $\therefore a_{5}, a_{7} \text{ and } a_{13} \text{ are in G.P}$   $(a_{7})^{2} = a_{5}, a_{13}$   $(a + 6d)^{2} = (a + 4d) (a + 12d)$   $a^{2} + 12ad + 36d^{2} = a^{2} + 16ad + 48d^{2}$   $12d^{2} + 4ad = 0 \Rightarrow 3d + a = 0$   $a = -3d \Rightarrow \frac{a}{d} = -3$ 

36. Option (c) is correct. Explanation:  $\therefore p, 1 \text{ and } q \text{ are A.P.}$   $\Rightarrow p+q=2 \qquad \dots (i)$   $p, 2 \text{ and } q \text{ are G.P} \Rightarrow pq = 4 \qquad \dots (ii)$ Now,  $\frac{2pq}{p+q} = \frac{8}{2} = 4$   $\therefore \frac{p+q}{2pq} = \frac{1}{4}$   $\therefore \frac{1}{p}, \frac{1}{4} \text{ and } \frac{1}{q} \text{ are in A.P.}$   $\therefore p, 4 \text{ and } q \text{ are in H.P.}$ Both statements are correct. 37. Option (d) is correct. Explanation:  $x = (1111)_2 = 2^3 + 2^2 + 2^1 + 1 = 15$  $y = (1001)_2 = 2^3 + 0 + 0 + 1 = 9$  $z = (110)_2 = 2^2 + 2^1 + 0 = 6$ Now,  $x^3 - y^3 - z^3 - 3xyz$  $= (15)^{3} - (9)^{3} - (6)^{3} - 3 \times 15 \times 9 \times 6$ = 3375 - 729 - 216 - 2430= 038. Option (a) is correct. Explanation: Cofactors: A = ei - hf, B = gf - di, C = dh - geD = ch - bi and G = bf - ecNow, bB + cC - dD - gG= bgf - bdi + cdh - cge - cdh + bdi - gbf + gec = 039. Option (a) is correct. Explanation:  $\Delta = \begin{vmatrix} k^2 + 2k & 2k+1 & 1 \\ 2k+1 & k+2 & 1 \\ 3 & 3 & 1 \end{vmatrix}$  $= (k^{2} + 2k)(k + 2 - 3) - (2k + 1)(2k + 1 - 3) + (6k)(2k + 1 - 3)$ +3 - 3k - 6 $= k^{3} - k^{2} + 2k^{2} - 2k - 4k^{2} + 4k - 2k + 2 + 3k - 3$  $= k^3 - 3k^2 + 3k - 1$  $= (k-1)^3$  $(k-1)^3 > 0 \Longrightarrow k > 1$ (i)  $(k-1)^3 < 0 \Rightarrow k < 1$ (ii)  $(k-1)^3 = 0 \Longrightarrow k = 1$ (iii) 40. Option (b) is correct. Explanation: 2 3 + i = 13-i 0 i-1-1 -1-i 1  $= 2(i^{2} - 1) - (3 + i)(3 - i + i - 1) + 1(3 - i)(i + 1)$  $= 2(-1-1) - (3+i) 2 + 3i - i^{2} + 3 - i$ = -4 - 6 - 2i + 3i + 1 + 3 - i= -6 = -6 + 0i = A + iB $\therefore A + B = -6 + 0 = -6$ 41. Option (b) is correct. *Explanation:*  $p + q + r = \sin 35^\circ + \sin 25^\circ + \sin 25^\circ$  $sin(-95^{\circ})$  $= \sin 35^\circ + \sin 25^\circ - \sin 95^\circ$ 

$$= \sin 35^\circ + 2\cos 60^\circ.\sin(-35^\circ)$$

$$=\sin 35^\circ - 2 \times \frac{1}{2} \sin 35^\circ = 0$$

42. Option (a) is correct. Explanation: pq + qr + rp = q(p + r) + rp  $= -q^{2} + rp = -\sin^{2} 25^{\circ} - \sin 95^{\circ} \cdot \sin 35^{\circ}$ ( $\therefore p + q + r = 0$ )

Μ

- $= \frac{1}{2} \left[ -2\sin^2 25^\circ 2\sin 95^\circ . \sin 35^\circ \right]$  $= \frac{1}{2} \left[ -1 + \cos 50^\circ + \cos 130^\circ - \cos 60^\circ \right]$  $=\frac{1}{2}\left[-1+\cos 50^\circ-\cos 50^\circ-\frac{1}{2}\right]$  $=\frac{-3}{4}$
- 43. Option (c) is correct.

**Explanation**:

$$(p+q+r)^{2} = p^{2} + q^{2} + r^{2} + 2(pq+qr+rp)$$
  

$$\Rightarrow \qquad 0 = p^{2} + q^{2} + r^{2} + 2\left(\frac{-3}{4}\right)$$
  

$$\Rightarrow p^{2} + q^{2} + r^{2} = \frac{3}{2}$$

$$\Rightarrow p^2 + q^2 + r^2 =$$

44. Option (a) is correct.

**Explanation**:

$$p = |\sin \alpha - \sin(\alpha - 90^{\circ})|$$
  
=  $|\sin \alpha + \cos \alpha|$   
=  $\sqrt{2} |\sin 45^{\circ} \sin \alpha + \cos 45^{\circ} \cos \alpha|$   
$$p = \sqrt{2} |\sin(45^{\circ} + \alpha)|$$
  
$$0 \le |\sin(45^{\circ} + \alpha)| \le 1$$
  
$$0 \le \sqrt{2} |\sin(45^{\circ} + \alpha)| \le \sqrt{2}$$
  
$$\therefore \text{Minimum value of } p \text{ is } 0$$

#### 45. Option (b) is correct.

- $p = \sqrt{2} |\sin 45^\circ + \alpha|$ Explanation:  $0 \le p \le \sqrt{2}$  $\Rightarrow$
- $\therefore$  Maximum value =  $\sqrt{2}$
- 46. Option (c) is correct. *Explanation:* a = 5 cm, b = 7 cm, c = 3 cm

$$\cos B = \frac{a^2 + c^2 - b^2}{2ac}$$
$$= \frac{25 + 9 - 49}{2 \times 5 \times 3} = \frac{-15}{2 \times 15} = \frac{-1}{2}$$
$$B = 120^{\circ}$$
$$\therefore A + C = 180^{\circ} - 120^{\circ} = 60^{\circ} \text{ (acute)}$$
So both statements are correct.

47. Option (c) is correct. **Explanation**:

*:*.

$$\cos B = \frac{a^2 + c^2 - b^2}{2ac}$$
$$= \frac{25 + 9 - 49}{2 \times 5 \times 3} = -\frac{1}{2}$$
$$B = 120^{\circ}$$

48. Option (a) is correct. Explanation:

Area of triangle = 
$$\frac{1}{2} \times ac \sin B$$
  
=  $\frac{1}{2} \times 5 \times 3 \times \sin 120^\circ$  =  $\frac{1}{2} \times 15 \times \sin 60^\circ$   
=  $\frac{1}{2} \times 15 \times \frac{\sqrt{3}}{2}$  =  $\frac{15\sqrt{3}}{4}$  cm<sup>2</sup>

49. Option (b) is correct. **Explanation**:

> $\frac{\cancel{30^{\circ}}}{45^{\circ}} \cancel{60^{\circ}}$   $P \leftarrow a \rightarrow Q \leftarrow b \rightarrow R \leftarrow x \rightarrow a$ N  $\tan 60^\circ = \frac{h}{r} \Rightarrow h = \sqrt{3}x$  $\tan 45^\circ = \frac{h}{QN} \Rightarrow QN = h$  $\tan 30^\circ = \frac{h}{PN}$  $PN = h\sqrt{3}$  $h + a = h\sqrt{3}$  $h = \frac{a}{\sqrt{3}-1} = \frac{a(\sqrt{3}+1)}{2}$

- PN =  $h\sqrt{3} = \frac{a(3+\sqrt{3})}{2}$
- 50. Option (a) is correct.

Explanation:

 $\Rightarrow$ 

 $\Rightarrow$ 

$$\tan 60^\circ = \frac{h}{x} \Rightarrow h = \sqrt{3}x$$
$$\tan 45^\circ = \frac{h}{b+x}$$
$$h = b + x \Rightarrow \sqrt{3}x = b + x$$
$$x = \frac{b(\sqrt{3}+1)}{2}$$

$$h = MN = \sqrt{3}x = \left(\frac{3+\sqrt{3}}{2}\right)k$$

51. Option (c) is correct. Explanation: P(Bonus introduced)

$$= \frac{3}{10} \times \frac{4}{9} + \frac{1}{2} \times \frac{2}{9} + \frac{4}{5} \times \frac{1}{3}$$

$$= \frac{2}{15} + \frac{1}{9} + \frac{4}{15} = \frac{6+5+12}{45} = \frac{23}{45}$$

52. Option (b) is correct. Explanation: F: Bonus introduced

$$\therefore \qquad P(A \setminus F) = \frac{\frac{2}{15}}{\frac{23}{45}} = \frac{2}{15} \times \frac{45}{23} = \frac{6}{23}$$

53. Option (a) is correct. Explanation:

New Mean 
$$=$$
  $\frac{50-5}{20} = \frac{45}{20} = 2.25$ 

54. Option (b) is correct. *Explanation:* When 5 is added to each observation then the standard deviation is not changed

$$\therefore$$
 New standard deviation =  $\frac{10}{20} = 0.5$ 

55. Option (b) is correct. **Explanation**:

$$P(B/A') = \frac{P(BAA')}{P(A')} = \frac{P(B) - P(B \cap A)}{1 - P(A)}$$
$$= \frac{\frac{1}{2} - \frac{1}{4}}{1 - \frac{1}{3}} = \frac{1}{4} \times \frac{3}{2} = \frac{3}{8}$$

56. Option (b) is correct.

**Explanation**: P(A'

57. Option (b) is correct. **Explanation**:

$$n(s) = 6 \times 6 = 36$$

Sum strictly greater than 7  $= \{(2,6), (3,5), (3,6), (4,4), (4,5), (4,6), (5,3), (5,4), (5,6$ (5, 5), (5, 6), (6, 2), (6, 3), (6, 4), (6, 5), (6, 6)n(E) = 15 $P(E) = \frac{15}{36} = \frac{5}{12}$ *:*.

58. Option (c) is correct. *Explanation:*  $P(X \ge 2) = 1 - P(X = 0) - P(X = 1)$  $= 1 - {^7C_0} \left(\frac{1}{5}\right)^0 \left(\frac{4}{5}\right)^7 - {^7C_1} \left(\frac{1}{5}\right)^1 \left(\frac{4}{7}\right)^6$ 

$$= 1 - \left(\frac{4}{5}\right)^{6} \left[\frac{4}{5} + \frac{7}{5}\right] = 1 - \left(\frac{11}{5}\right) \left(\frac{4}{5}\right)^{6}$$

59. Option (b) is correct. **Explanation**:

 $\Rightarrow$ 

 $\Rightarrow$ 

 $\Rightarrow$ 

$$\overline{x} = xp = 200 \qquad \dots (i)$$

$$\sigma^2 = xpq = 160 \dots$$

$$q = \frac{160}{200} = \frac{4}{5}$$

$$p = 1 - \frac{4}{5} = \frac{1}{5}$$

$$n = 1000$$

60. Option (c) is correct. Explanation:

$$sum = s_{15} - s_7$$
  
=  $\frac{15 \times 16 \times 31}{6} - \frac{7 \times 8 \times 15}{6}$   
=  $1240 - 140 = 1100$   
mean =  $\frac{1100}{6} = 137.5$ 

$$=\frac{1100}{8}=1$$

61. Option (d) is correct. **Explanation**:

$$y = \sin^{-1} \left( x - \frac{4x^3}{27} \right)$$
$$= \sin^{-1} \left[ 3 \cdot \frac{x}{3} - 4 \left( \frac{x}{3} \right)^3 \right]$$
$$= 3 \sin^{-1} \frac{x}{3}$$

62. Option (c) is correct. **Explanation**:

$$y = 3 \sin^{-1} \frac{x}{3}$$
$$\frac{dy}{dx} = 3 \frac{1}{\sqrt{1 - \frac{x^2}{9}}} \times \frac{1}{3} = \frac{3}{\sqrt{9 - x^2}}$$

63. Option (c) is correct.

Explanation: 
$$\lim_{x \to 0} \frac{\sqrt{x^2 + 9} - 3}{\sqrt{x^2 + 16} - 4}$$
$$= \lim_{x \to 0} \frac{x^2 + 9 - 9}{x^2 + 16 - 16} \times \frac{\sqrt{x^2 + 16} + 4}{\sqrt{x^2 + 9} + 3}$$
$$= \frac{\sqrt{16} + 4}{\sqrt{9} + 3} = \frac{8}{6} = \frac{4}{3}$$

64. Option (d) is correct. Explanation:  $f(x) = x^2 + 9$  $f(x) = 2x = 0 \Rightarrow x = 0$ 

 $\infty$ 

∴ f(x) is increasing on  $[0, \infty]$ and f(x) is decreasing on  $(-\infty, 0)$ So, f(x) is minimum at x = 0Hence both statements are wrong.

65. Option (d) is correct. *Explanation:* 

$$\frac{f(4)}{f(2)} = f\left(\frac{4}{2}\right) = f(2) \Rightarrow f(4) = 3 \times 3 = 9$$
$$\frac{f(16)}{f(4)} = f(4) \Rightarrow f(16) = 9 \times 9 = 81$$

66. Option (c) is correct. *Explanation:* 

 $\frac{f(4)}{f(2)} = f(2) \Rightarrow f(4) = 3 \times 3 = 9$  $\frac{f(2)}{f(2)} = f(1) \Rightarrow f(1) = 1$  $f(1) f(4) = 1 \times 9 = 9$ 

- 67. Option (d) is correct. *Explanation:*  $f(0) = f(0 \times 5) = f(0 + 5) = f(5) = 10$
- 68. Option (c) is correct. *Explanation:*

Now,

- f(0.5) = f(0 + 5) = f(0) = f(5) = 10  $f(0.20) = f(0 + 20) \Rightarrow f(0) = f(20) = 10$   $f(0 \times -20) = f(0 - 20) \Rightarrow f(0) = f(-20) = 10$  $\therefore f(20) + f(-20) = 10 + 10 = 20$
- 69. Option (b) is correct. *Explanation:*

$$\int_{\sqrt{2}}^{\sqrt{3}} [x^2] dx = \int_{\sqrt{2}}^{\sqrt{3}} 2dx = 2[x]_{\sqrt{2}}^{\sqrt{3}}$$
$$= 2(\sqrt{3} - \sqrt{2})$$

70. Option (a) is correct. *Explanation:* 

$$\int_{\sqrt{2}}^{2} f(x)dx = \int_{\sqrt{2}}^{2} [x^{2}]dx = \int_{\sqrt{2}}^{\sqrt{3}} 2dx + \int_{\sqrt{3}}^{2} 3dx$$
$$= 2[x]_{\sqrt{2}}^{\sqrt{3}} + 3[x]_{\sqrt{3}}^{2}$$
$$= 2\sqrt{3} - 2\sqrt{2} + 6 - 3\sqrt{3}$$
$$= 6 - 2\sqrt{2} - \sqrt{3}$$

71. Option (b) is correct. Explanation:  $\therefore A^2 + B^2 + C^2 = 0$  $\therefore A = B = C = 0$ Now,  $\begin{vmatrix} 1 & \cos C & \cos B \\ \cos C & 1 & \cos A \\ \cos B & \cos A & 1 \end{vmatrix} = \begin{vmatrix} 1 & 1 & 1 \\ 1 & 1 & 1 \\ 1 & 1 & 1 \end{vmatrix} = 0$ 72. Option (a) is correct. *Explanation:*  $|_{x+1} \quad \omega$  $\begin{vmatrix} \omega & x + \omega^2 & 1 \\ \omega^2 & 1 & x + \omega \end{vmatrix} = 0$ (Applying  $C_1 \rightarrow C_1 + C_2 + C_3$ )  $x+1+\omega+\omega^2$   $\omega$   $\omega^2$  $x + 1 + \omega + \omega^2 \quad x + \omega^2 \quad 1 = 0$  $x+1+\omega+\omega^2$  1  $x+\omega$ ω  $\begin{vmatrix} x & x + \omega^2 & 1 \\ x & 1 & x + \omega \end{vmatrix} = 0$  $\begin{vmatrix} 1 & \omega & \omega^2 \\ x & 1 & x + \omega^2 & 1 \end{vmatrix} = 0$ 1 1  $x + \omega$  $\therefore x = 0$ 73. Option (a) is correct. **Explanation**:  $\left(\frac{\sqrt{3}+i}{\sqrt{3}-i}\right)^3 = \left(\frac{\left(\sqrt{3}+i\right)^2}{2+1}\right)^3$  $=\left(\frac{\sqrt{3}}{2}+\frac{1}{2}i\right)^6$  $=\left(\cos\frac{\pi}{6}+i\sin\frac{\pi}{6}\right)^{6}$ 

$$=\cos\pi + i\sin\pi = -1$$

74. Option (c) is correct.

Explanation:  $x^2 - x + 1 = 0 \Rightarrow x = \frac{1 \pm \sqrt{3}i}{2}$ if  $x = \frac{1 + \sqrt{3}i}{2}$  then  $\frac{1}{x} = \frac{1 - \sqrt{3}i}{2}$ Now  $x - \frac{1}{x} = \sqrt{3}i$   $\left(x - \frac{1}{x}\right)^2 + \left(x - \frac{1}{x}\right)^4 + \left(x - \frac{1}{x}\right)^8$ = -3 + 9 + 81 = 87 75. Option (c) is correct. Explanation: CPTL AIA 1 3 Total words =  $\frac{4!}{2!} \times 4!$ =  $\frac{24 \times 24}{2} = 288$ 

- 76. Option (a) is correct. *Explanation:* Let  $amp(z) = \theta$   $\therefore \qquad amp(\overline{z}) = -\theta$ Now  $amp(z) + amp(\overline{z}) = 0$
- 77. Option (c) is correct. *Explanation:* Number of diagonals  $= {}^{n}C_{2} - n = 20$

$$= \frac{n(n-1)}{2} - n$$

$$= 20$$

$$\Rightarrow \qquad n^2 - 3n - 40 = 0$$

$$\Rightarrow \qquad n = 8$$

- 78. Option (c) is correct.*Explanation:* Number of arrangements= 3!2! = 12
- 79. Option (c) is correct. *Explanation:*

*:*.

$$x + y + z = 5$$
  
(1, 1, 3)  $\rightarrow \frac{3!}{2!} = 3$  ways  
(1, 2, 2)  $\rightarrow \frac{3!}{2!} = 3$  ways

- Total ways = 3 + 3 = 6**80. Option (c) is correct.** 
  - Explanation:

$$T_{r+1} = {}^{n}C_{r} \left(\frac{1}{3^{2}}\right)^{12-r} \left(\frac{1}{5^{4}}\right)^{r}$$
$$= {}^{12}C_{r} 3^{\frac{12-r}{2}} 5^{\frac{r}{4}}$$

for rational term  $\frac{12-r}{2}$  and  $\frac{r}{4}$  is integer.

- $\therefore$  Possible values of r = 0, 4, 8, 12
- 81. Option (a) is correct. *Explanation:*

$$m_1 = \frac{-m^2}{n}$$
 and  $m_2 = \frac{-n^2}{-m} = \frac{n^2}{m}$ 

for perpendicular

$$-\frac{m^2}{n} \times \frac{n^2}{m} = -1 \Longrightarrow mn - 1 = 0$$

#### 82. Option (d) is correct.

Explanation:

$$\sqrt{p^{2} + 1} = \sqrt{q^{2} + 1} = \sqrt{(p - 1)^{2} + (q - 1)^{2}}$$

$$\sqrt{p^{2} + 1} = \sqrt{q^{2} + 1} \Rightarrow p = q [\therefore p, q \in (0, 1)]$$
Now,  $\sqrt{q^{2} + 1} = \sqrt{(p - 1)^{2} + (q - 1)^{2}}$ 

$$\Rightarrow p^{2} + 1 = 2 (p - 1)^{2}$$

$$\Rightarrow p^{2} - 4p + 1 = 0 \Rightarrow p = 2 \pm \sqrt{3}$$
Since,  $0 
Now,  $p + q = 2(2 - \sqrt{3}) = 4 - 2\sqrt{3}$$ 

83. Option (a) is correct.

Explanation: 
$$a = BC = \sqrt{(2-0)^2 + (0-0)^2} = 2$$
  
 $b = AC = \sqrt{(2-1)^2 + (0-1)^2} = \sqrt{2}$   
 $c = AB = \sqrt{(1-0)^2 + (1-0)^2} = \sqrt{2}$   
 $\therefore$  Coordinate of incentive  
 $= \left(\frac{ax_1 + bx_2 + cx_3}{a + b + c}, \frac{ay_1 + by_2 + cy_3}{a + b + c}\right)$   
 $= \frac{2(1) + \sqrt{2}(0) + \sqrt{2}(2)}{2 + \sqrt{2} + \sqrt{2}}, \frac{2(1) + \sqrt{2}(0) + \sqrt{2}(0)}{2 + \sqrt{2} + \sqrt{2}}$   
 $= \left(\frac{2 + 2\sqrt{2}}{2 + 2\sqrt{2}}, \frac{2}{2 + 2\sqrt{2}}\right) = (1, \sqrt{2} - 1)$ 

84. Option (b) is correct. *Explanation:* Coordinate of P =  $\left(\frac{3+1}{2}, \frac{-1+1}{2}\right)$ = P(2, 0)Slope of AB =  $\frac{1+1}{1-3} = -1$ Equation of AB is  $y-1 = -1 (x-1) \Rightarrow x + y - 2 = 0$ Distance from Q(x, y) $\frac{x+y-2}{\sqrt{2}} = \sqrt{2}$  $x + y - 2 = 2 \Longrightarrow x + y = 4$ ...(i) Slope of PQ =  $\frac{y}{x-2}$  $\Rightarrow$  PQ  $\perp$  AB  $\therefore (-1)\left(\frac{y}{x-2}\right) = -1 \Rightarrow y = x-2$ From (i)  $x + x - 2 = 4 \Rightarrow x = 3$  and y = 1Q(3, 1)

85. Option (d) is correct. *Explanation:* 

Slope of AD = 
$$\frac{6-2}{-2-1} = \frac{4}{-3}$$

$$\therefore$$
 Slope of BC =  $\frac{3}{4}$ 

Equation of BC is

$$y-6 = \frac{3}{4} (x+2) \Rightarrow 3x-4y+30 = 0$$

86. Option (b) is correct. *Explanation:* 

Radius = 
$$\frac{10}{2}$$
 = 5 cm

On solving x + y = 0 and x - y = 0we get centre (0, 0) Now, the equation of circle  $x^2 + y^2 = 25$ 

87. Option (c) is correct. *Explanation:* 



Equation of circle is  

$$x^{2} + y^{2} + 2x + 2y + 1 = 0$$
  
 $\therefore$  centre = (-1, -1)  
Radius =  $\sqrt{1+1-1} = 1$   
Diagonal = diameter  
 $\sqrt{2a} = 2 \Rightarrow a = \sqrt{2}$ 

Since the sides of the square are parallel to the co-ordinate axes, the vertices can be found by

moving  $\frac{a}{2}$  units from the centre along the axes.

: One of the vertices is

$$\left(-1+\frac{1}{\sqrt{2}},-1-\frac{1}{\sqrt{2}}\right)$$

**88.** Option (d) is correct. *Explanation:* Scope of tangent = tan 45° = 1

$$y^{2} = 4x \Rightarrow 2y \frac{dy}{dx} = 4$$
  
$$\Rightarrow \qquad \frac{dy}{dx} = \frac{4}{2y} = 1 \Rightarrow y = 2$$
  
putting in  $y^{2} = 4x \Rightarrow x = 1$   
 $\therefore$  Point of contact = (1, 2)

89. Option (b) is correct. *Explanation:*  $25x^2 - 75y^2 = 225$ 

$$\frac{x^2}{9} - \frac{y^2}{3} = 1$$
  

$$\therefore \qquad a^2 = 9 \text{ and } b^2 = 3$$
  

$$c^2 = a^2 + b^2 = 9 + 3 = 12$$
  

$$c = 2\sqrt{3}$$

Distance between the two foci =  $2c = 4\sqrt{3}$ 

#### 90. Option (a) is correct.

*Explanation:* We know that the parametric point of ellipse is  $(a \sin \alpha) b \cos \alpha$ 

$$\therefore a = 3 \text{ and } b = 5$$

$$b^{2} = a^{2} (1 - e^{2}) \Rightarrow \frac{25}{9} = 1 - e^{2}$$
  
 $e^{2} = 1 - \frac{25}{9} = \frac{16}{9} \Rightarrow e = \frac{4}{2}$ 

*Explanation:* Total number of students whose height is less than or equal to 165 cm = 12 + 15+ 24 = 51

#### 92. Option (c) is correct.

Explanatio	n:		
C.I.	fi	C.F	
160–162	12	12	4.11
162–164	15	27	
164–166	24(M)	51	Median Class
166-168	13	64	

$$\frac{N}{2} = \frac{64}{2} = 32$$
$$\frac{N}{2} - C.F$$

Median = 
$$l + \frac{2}{f} \times h$$

$$= 164 + \frac{32 - 27}{24} \times 2$$
$$= 164 + \frac{5}{12} = 164.41 \text{ cm}$$

93. Option (d) is correct.

Explanation: Mode =  $l + \frac{f_1 - f_0}{2f_1 - f_0 - f_2} \times h$ =  $164 + \frac{24 - 15}{48 - 15 - 13} \times 2$ =  $164 + \frac{9}{20} \times 2$ 

= 164.9 cm

**94. Option (c) is correct.** *Explanation:* Histogram is made from group frequency data.

## 95. Option (b) is correct. *Explanation:*

Variance of X = 
$$\frac{\Sigma X^2}{N} - \left(\frac{\Sigma X}{N}\right)^2$$
  
=  $\frac{900}{50} - \left(\frac{200}{50}\right)^2$   
=  $18 - 16 = 2$   
Variance of Y =  $\frac{\Sigma Y^2}{N} - \left(\frac{\Sigma Y}{N}\right)^2$   
=  $\frac{1400}{50} - \left(\frac{250}{50}\right)^2$   
=  $28 - 25 = 3$ 

$$\therefore$$
 Variance (X) < Variance (Y)

96. Option (b) is correct. *Explanation:* 

$$C.V(X) = \frac{\sigma}{M} \times 100$$
$$= \frac{\sqrt{2}}{50} \times 100 = 2\sqrt{2}$$
$$C.V(Y) = \frac{\sigma}{M} \times 100$$
$$= \frac{\sqrt{3}}{50} \times 100 = 2\sqrt{3}$$

 $\therefore$  C.V(X) < C.V(Y)

- 97. Option (c) is correct. *Explanation:* n = 6,  $p = k \Rightarrow q = 1 - k$ 
  - Now, 9.P(X = 4) = P(X = 2) 9.<sup>6</sup>C<sub>4</sub>k<sup>4</sup>(1-k)<sup>2</sup> = <sup>6</sup>C<sub>2</sub>k<sup>2</sup>(1-k)<sup>4</sup> 9k<sup>2</sup> = (1-k)<sup>2</sup> (:: <sup>6</sup>C<sub>4</sub> = <sup>6</sup>C<sub>2</sub>) 3k = 1-k \Rightarrow k =  $\frac{1}{4}$
- 98. Option (a) is correct. *Explanation:*

$$P(x = 3) = {}^{6}C_{3}(k)^{3} (1 - k)^{3}$$
$$= \frac{6.5.4}{3.2.1} \left(\frac{1}{4}\right)^{3} \left(\frac{3}{4}\right)^{3}$$
$$= 20 \left(\frac{3}{16}\right)^{3} = 20 \times \frac{27}{16 \times 16 \times 16}$$
$$= \frac{135}{1024}$$

## 99. Option (a) is correct. *Explanation:*

$$n(S) = {}^{11}C_6$$
  
 $n(E) = {}^7C_3 \times {}^4C_3$ 

$$P(E) = \frac{{}^{7}C_{3} \times {}^{4}C_{3}}{{}^{11}C_{6}} = \frac{10}{33}$$

100. Option (d) is correct.

Explanation: P(E)  
= 
$$\frac{{}^{4}C_{2} \times^{7}C_{4} + {}^{4}C_{3} \times^{7}C_{3} + {}^{4}C_{4} \times^{7}C_{2}}{{}^{11}C_{6}}$$

$$=\frac{53}{66}$$

101. Option (b) is correct.

Explanation: 
$$y = (1 - \cos x)^{-1} = \frac{1}{1 - \cos x}$$
  

$$= \frac{1}{2\sin^2 \frac{x}{2}} = \frac{1}{2}\operatorname{cosec}^2 \frac{x}{2}$$

$$\therefore \operatorname{cosec} \frac{x}{2} \leftarrow (-\infty, -1) \cup (1, \infty)$$

$$\operatorname{cosec}^2 \frac{x}{2} \leftarrow (1, \infty)$$

$$\Rightarrow \frac{1}{2}\operatorname{cosec}^2 \frac{x}{2} \leftarrow (0.5, \infty)$$
Range =  $(0.5, \infty)$   
102. Option (b) is correct.

Explanation:

$$I = \int y dx = \frac{1}{2} \int \operatorname{cosec}^2 \frac{x}{2} dx$$
$$= \frac{-\frac{1}{2} \cot \frac{x}{2}}{\frac{1}{2}} + C$$
$$= -\cot \frac{x}{2} + C$$

103. Option (b) is correct. *Explanation:* 

$$\lim_{x \to 0} \{f(x) \cdot g(x)\} = \lim_{x \to 0} \{f(x) \cdot g(x)\}$$

$$\mathbf{L.H.L} = \lim_{h \to 0} \sin[0-h] |0-h|$$

$$= \lim_{h \to 0} \sin[0-h] \cdot 0 = \mathbf{0}$$

$$\mathbf{R.H.L} = \lim_{h \to 0} \sin[0+h] |0+h|$$

$$= \lim_{h \to 0} \sin 0 \cdot h = \mathbf{0}$$

$$\therefore \quad \lim_{x \to 0} \{f(x)g(x)\} = 0$$

#### 104. Option (d) is correct.

Explanation: 
$$\lim_{x \to 0} \frac{\sin[x]}{[x]}$$
  
L.H.L = 
$$\lim_{h \to 0} \frac{\sin[0-h]}{(0-h)} = \text{infinity}$$
  
R.H.L = 
$$\lim_{h \to 0} \frac{\sin[0+h]}{(0+h)}$$
$$= \lim_{h \to 0} \frac{\sin 0}{(h)} = 0$$

L.H.L  $\neq$  R.H.L, limit does not exist.

#### 105. Option (c) is correct.

*Explanation:* Domain of f(x) = |x-3| is  $(-\infty, \infty)$ 

#### 106. Option (d) is correct.

**Explanation**:



Required area

$$= 3 \times 6 - \frac{1}{2} \times 3 \times 3 - \frac{1}{2} \times 3 \times 3$$

= 18 - 9 = 9 square units

#### 107. Option (c) is correct.

Explanation:

$$f(x) = px + q$$
  
put x = 1 and y = 1

$$p + q = 1$$

#### 108. Option (a) is correct.

Explanation:

 $\therefore$  f(x) = px + q is linear polynomial so, f(x) is one-one

Range =  $\{1, 4, 7, 10\}$ 

$$codomain = N$$

So it is not onto.

#### 109. Option (a) is correct.

Explanation: 
$$\lim_{x \to 1} f(f(x)) = \lim_{x \to 1} (x^2 - 1)^2 - 1$$
  
=  $(1 - 1)^2 - 1 = 0 - 1 = -1$ 

110. Option (c) is correct.



Required area =  $\left| \int_{-1}^{1} (x^2 - 1) dx \right|$ 

$$= \left\| \left[ \frac{x^3}{3} - x \right]_{-1}^{1} \right\| = \left\| \left( \frac{1}{3} - 1 \right) - \left( -\frac{1}{3} + 1 \right) \right\|$$

$$| 2 \ 2 | | 4 | 4$$

$$= \left| -\frac{2}{3} - \frac{2}{3} \right| = \left| -\frac{1}{3} \right| = \frac{4}{3}$$
 sq. units

111. Option (c) is correct.

Explanation: We know that  
If 
$$x = \sec \theta - \cos \theta$$
 and  $y = \sec^n \theta - \cos^n \theta$   
then  $(x^2 + 4) \left(\frac{dy}{dx}\right)^2 - n^2(y^2 + 4) = 0$   
 $(x^2 + 4) \left(\frac{dy}{dx}\right)^2 - (4)^2(y^2 + 4) = 0$   
 $\left(\frac{dy}{dx}\right)^2 = \frac{16(y^2 + 4)}{x^2 + 4}$ 

112. Option (c) is correct.

Explanation: 
$$\therefore \left(\frac{dy}{dx}\right)^2 = \frac{16(y^2 + 4)}{x^2 + 4}$$
  
$$2\left(\frac{dy}{dx}\right)\left(\frac{d^2y}{dx^2}\right)$$
$$= \frac{16(2y)(x^2 + 4)\frac{dy}{dx} - 16(y^2 + 4)(2x)}{(x^2 + 4)^2}$$

$$\frac{dy}{dx} \left(\frac{d^2y}{dx^2}\right) (x^2 + 4)^2 = 16y(x^2 + 4)\frac{dy}{dx} - 16x(y^2 + 4)$$
$$\frac{dy}{dx} \left(\frac{d^2y}{dx^2}\right) (x^2 + 4)^2 - 16y(x^2 + 4)\frac{dy}{dx} = -16x(y^2 + 4)$$

 $\frac{(x^2+4)}{y^2+4}\frac{dy}{dx}\left((x^2+4)\frac{d^2y}{dx^2} - 16y\right) = -16x$ 

113. Option (c) is correct.

$$\Delta A = \frac{\pi}{x} = -\frac{\pi}{3}$$
$$\angle A = \frac{\pi}{3}$$

114. Option (a) is correct.

Explanation: Maximum area

$$=\frac{1}{2} \times y \times x = \frac{\sqrt{3}}{2}$$
 sq. units

115. Option (d) is correct.

**Explanation**:

$$(x + y)^{p+q} = x^{p}y^{q}$$
  

$$\therefore (p+q) \log (x+y) = p\log x + q\log y$$
  

$$\frac{p+q}{x+y} \left(1 + \frac{dy}{dx}\right) = \frac{p}{x} + \frac{q}{y}\frac{dy}{dx}$$
  

$$\left(\frac{p+q}{x+y} - \frac{q}{y}\right)\frac{dy}{dx} = \frac{p}{x} - \frac{p+q}{x+y}$$
  

$$\frac{py+qy-qx-qy}{y(x+y)}\frac{dy}{dx} = \frac{px+py-px-qx}{x(x+y)}$$
  

$$\frac{py-qx}{y}\frac{dy}{dx} = \frac{py-qx}{x}$$
  

$$\therefore \qquad \frac{dy}{dx} = \frac{y}{x}$$

which is independent of both *p* and *q*.

116. Option (a) is correct.

*Explanation:* Since  $\frac{dy}{dx}$  is independent of both p and q. So for p + q = 10

$$\frac{dy}{dx} = \frac{y}{x}$$

117. Option (a) is correct.

Explanation:

*:*..

$$\frac{dy}{dx} = 4 \Rightarrow \int dy = \int 4dx$$
$$y = 4x + c$$

 $\therefore$  it passes through (0, 0) then c = 0

y = 4x*:*.. Hence it is an equation of a straight line passing through (1, 4)

118. Option (c) is correct.



119. Option (c) is correct. Explanation:

$$f(x) = \begin{cases} x^3 & -1 < x < 1\\ x^2 & x \in (-\infty, -1) \cup (1, \infty) \end{cases}$$
$$f(x) = \begin{cases} 3x^2 & -1 < x < 1\\ 2x & x \in (-\infty, -1) \cup (1, \infty) \end{cases}$$
$$\lim_{x \to 0} f'(x) = 3(0) = 0$$

120. Option (d) is correct.

**Explanation**:

*:*..

L.H.S = 
$$\lim_{x \to 1^{-}} x^2 = (-1)^2 = 1$$
  
R.H.S =  $\lim_{x \to -1^{+}} x^3 = (-1)^3 = -1$   
 $\therefore$  L.H.S  $\neq$  R.H.S  
So  $f(x)$  is discontinuous at  $x = -1$   
L.H.D =  $3(1) = 3$   
R.H.D =  $2(1) = 2$   
 $\therefore$  L.H.D  $\neq$  R.H.D  
So,  $f(x)$  is not differentiable at  $x = 1$   
Hence neither I nor II is true.